

AI Tutorials Solution

Machine Learning

1.

(a) For Outcome, $I(p, n) = I(10, 6) = -(10/16) \log_2(10/16) - (6/16) \log_2(6/16) = 0.954434$

(b) SPLIT ON "TIME"

For (TIME=Evening): $I(2, 0) = 0$

For (TIME=Day and Night): $I(7, 4) = 0.946$

For (TIME=Day): $I(1, 2) = 0.918$

Remainder(TIME) = $(2/16)*I(2,0) + (11/16)*I(7,4) + (3/16)*I(1,2) = 0.8225$

$IG(\text{TIME}) = 0.954434 - 0.8225 = 0.132$

SPLIT ON "MATCH TYPE"

For (MATCH TYPE=T20): $I(3, 3) = 1.0$

For (MATCH TYPE=ODI): $I(6, 1) = 0.592$

For (MATCH TYPE=Test): $I(1, 2) = 0.918$

Remainder(MATCH TYPE) = $(6/16)*I(3,3) + (7/16)*I(6,1) + (3/16)*I(1,2) = 0.8061$

$IG(\text{MATCH TYPE}) = 0.954434 - 0.8061 = 0.148$

SPLIT ON "PITCH TYPE"

For (PITCH TYPE=Fast): $I(4, 0) = 0$

For (PITCH TYPE=Dusty): $I(2, 3) = 0.971$

For (PITCH TYPE=Bouncy): $I(4, 1) = 0.722$

For (PITCH TYPE=Neutral): $I(0, 2) = 0$

Remainder(PITCH TYPE) = $(4/16)*I(4,0) + (5/16)*I(2,3) + (5/16)*I(4,1) + (2/16)*I(0,2) = 0.529$

$IG(\text{PITCH TYPE}) = 0.954434 - 0.529 = 0.425$

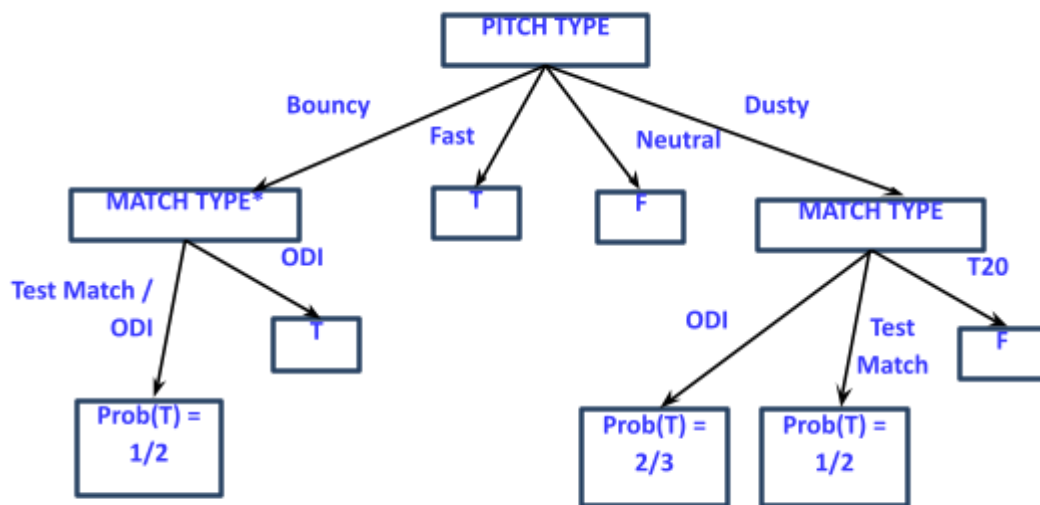
We choose PITCH TYPE because it yields the maximum information gain.

$$(c) \quad remainder(PITCH\ TYPE) = \sum_{i=1}^v \frac{p_i+n_i}{p+n} I\left(\frac{p_i}{p_i+n_i}, \frac{n_i}{p_i+n_i}\right)$$

$$IG(PITCH\ TYPE) = I\left(\frac{p}{p+n}, \frac{n}{p+n}\right) - remainder(PITCH\ TYPE)$$

$$IG(PITCH\ TYPE) = 0.425$$

(d)



*We could also have used TIME here

(e) India will win with a probability of 2/3.

2.

a. $H1 = \text{ReLU}([-1,0]*[1,1] + 0) = \text{ReLU}(-1) = 0$
 $H2 = \text{ReLU}([-1,1]*[1,1] + 0) = \text{ReLU}(0) = 0$

$O1 = \text{ReLU}([0,-1]*[0,0] + 1) = \text{ReLU}(1) = 1$
 $O2 = \text{ReLU}([-1,1]*[0,0] + 1) = \text{ReLU}(1) = 1$

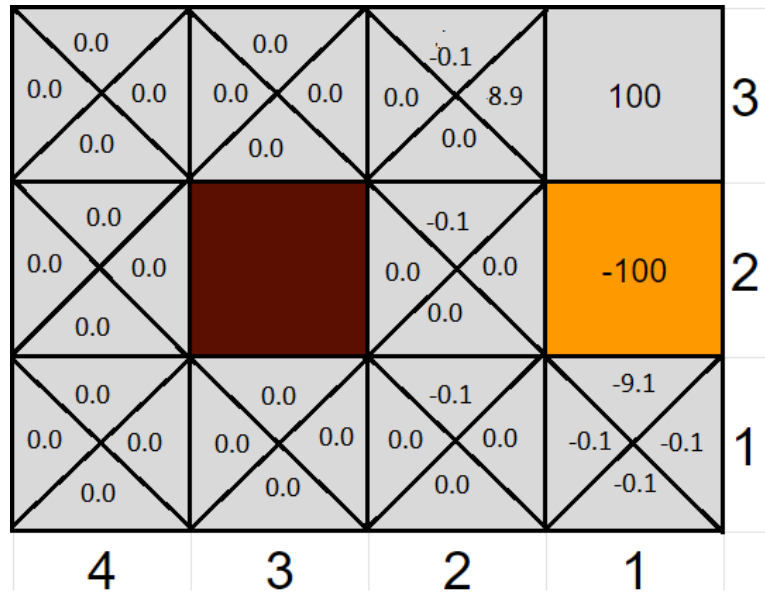
b. $\text{MSE}(O1) = (1-1)^2 = 0$
 $\text{MSE}(O2) = (0-1)^2 = 1$
 $\text{LOSS} = 0+1 = 1$

c. $O1 = \text{Sigmoid}([0,-1]*[0,0] + 1) = \text{Sigmoid}(1) = 0.731$
 $O2 = \text{Sigmoid}([-1,1]*[0,0] + 1) = \text{Sigmoid}(1) = 0.731$

$\text{MSE}(O1) = (1-0.731)^2 = 0.072$
 $\text{MSE}(O2) = (0-0.731)^2 = 0.534$
 $\text{LOSS} = 0.072+0.534 = 0.606$

3.

a.



b.

